



Scripting Languages

Simple approach to 3D graphics:

- basic 3D projection
- drawing 3D objects
- rotating 3D objects
- exercises

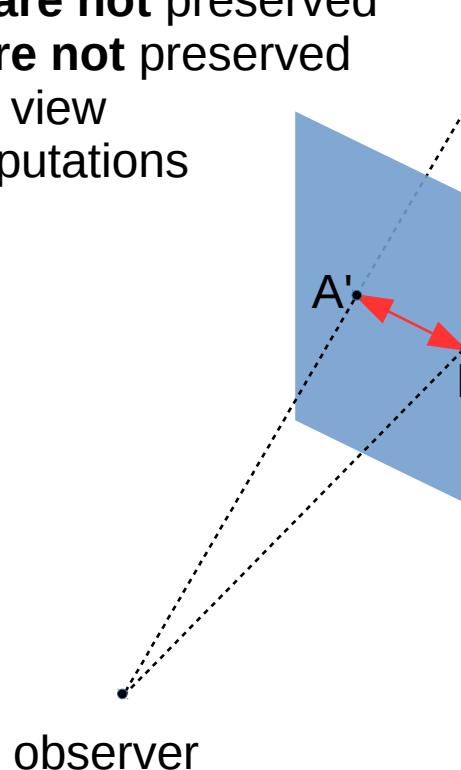


Viewing 3D graphics

- conversion: $(x, y, z) \rightarrow (x', y')$
- projection onto 2D plane

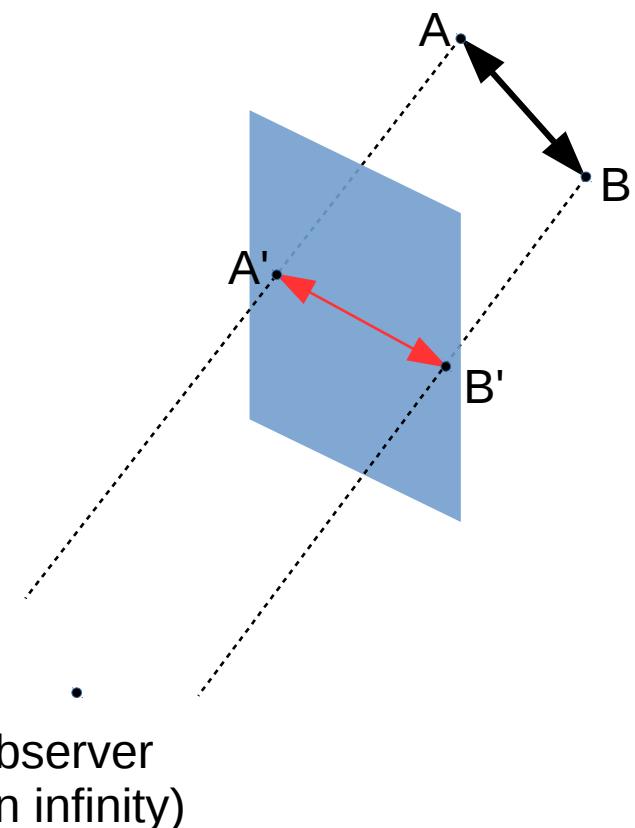
Perspective projection

- parallel lines **are not** preserved
- proportions **are not** preserved
- more realistic view
- complex computations



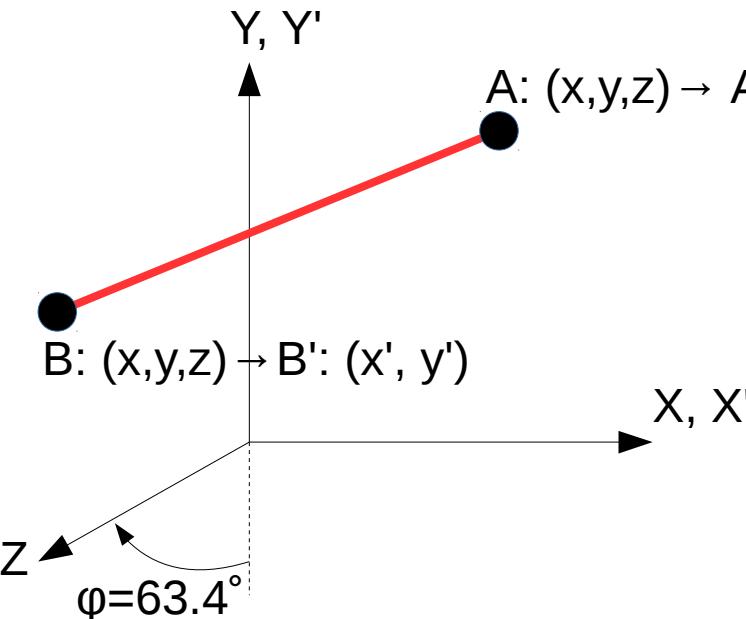
Parallel projection

- parallel lines **are** preserved
- proportions **are** preserved
- less realistic view (technical)
- **easy computations**





Cabinet (parallel) projection



$$x' = x - z \sin(\phi)k$$
$$y' = y - z \cos(\phi)k$$

k - length scaling factor ($= \frac{1}{2}$)

```
k = 0.5 # projection scale
phi = math.radians(63.4) # try also 45
sinphi = math.sin(phi)
cosphi = math.cos(phi)
```

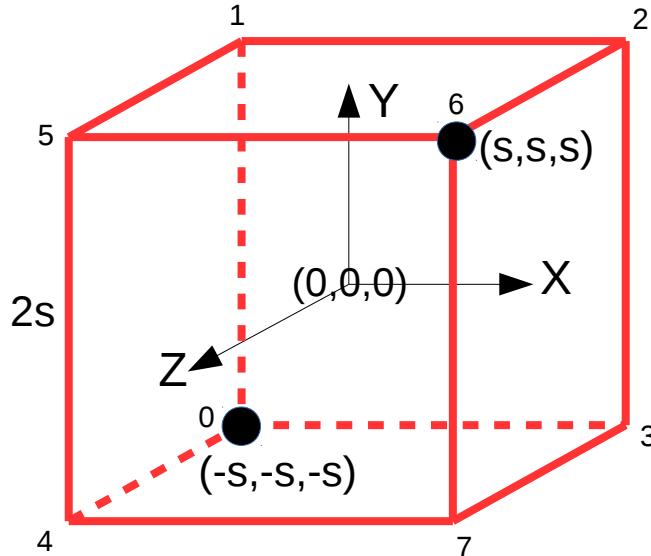
```
def drawline3d(a, b, w = 1):      # a, b -> ap, bp
    xa, ya, za = a[0], a[1], a[2]
    xb, yb, zb = b[0], b[1], b[2]

    # convert 3d to 2d with cabinet projection
    xap = xa - za*sinphi *k
    yap = ya - za*cosphi *k
    xbp = xb - zb*sinphi *k
    ybp = yb - zb*cosphi *k

    # convert to pygame-screen coordinates and draw
    s1, s2 = (win.centerx+xap, win.centery-yap), (win.centerx+xbp, win.centery-ybp)
    pygame.draw.line(scr, black, s1, s2, w)
```



Cube



Origin of coordinate system $(0,0,0)$ located in the center of the figure

Cube:

- 8 corners (points: P0 ... P7),
- 12 edges (lines: Px, Py)
- 24 drawing points (pairwise)

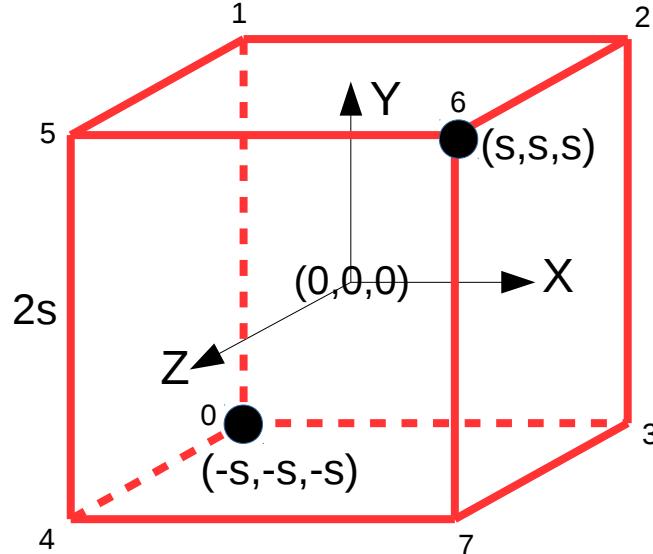
$s = 100$

$P_0, P_1, P_2, P_3 = (-s, -s, -s), (-s, s, -s), (s, s, -s), (s, -s, -s)$
 $P_4, P_5, P_6, P_7 = (-s, -s, s), (-s, s, s), (s, s, s), (s, -s, s)$

`cube = (P0, P1, P1, P2, P2, P3, P3, P0,
 P4, P5, P5, P6, P6, P7, P7, P4,
 P0, P4, P1, P5, P2, P6, P3, P7)`



Cube



```
cube = ( P0,P1, P1,P2, P2,P3, P3,P0,
          P4,P5, P5,P6, P6,P7, P7,P4,
          P0,P4, P1,P5, P2,P6, P3,P7 )
```

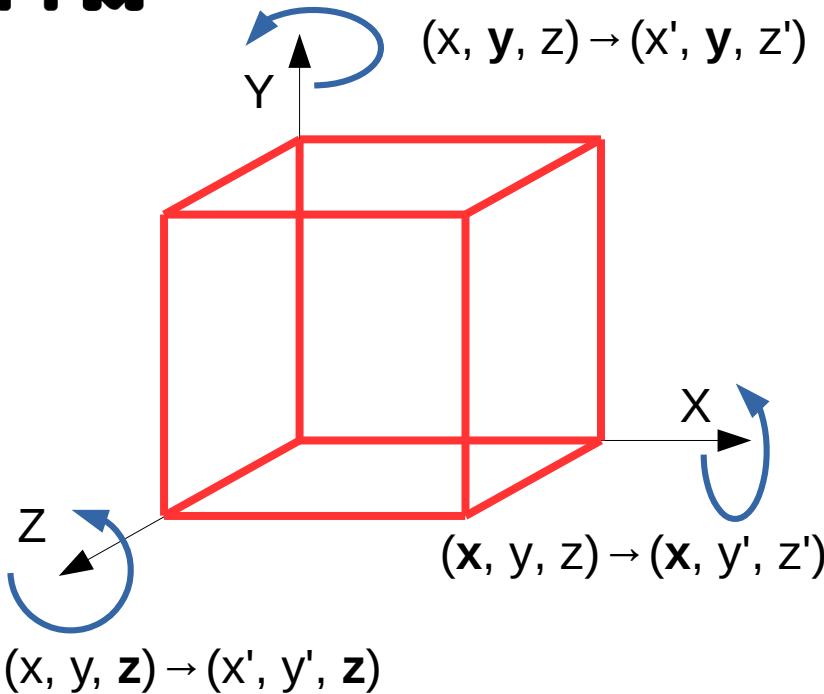
```
drawfigure3d(cube)
```

```
def drawfigure3d(figure):
    even = figure[0::2]
    odd = figure[1::2]

    #read points in pairs
    for a, b in zip(even, odd):
        drawline3d(a, b)
```



3D rotation



$$\begin{aligned}x' &= x \cos(\alpha) - y \sin(\alpha) \\y' &= x \sin(\alpha) + y \cos(\alpha) \\z' &= z\end{aligned}$$

```
cube = rotx(cube, a)
cube = roty(rotx(cube, a), a)
cube = rotz(roty(rotx(cube, a), a), a)
```

Rotation in 3D space can be composed of three 2D rotations

```
def rotx(fig, a):
    newfig = []
    sin, cos = math.sin(a), math.cos(a)
    for x, y, z in fig:
        newfig.append((x, y*cos-z*sin, y*sin+z*cos))
    return newfig

def roty(fig, a):
    newfig = []
    sin, cos = math.sin(a), math.cos(a)
    for x, y, z in fig:
        newfig.append((x*cos+z*sin, y, -x*sin+z*cos))
    return newfig

def rotz(fig, a):
    newfig = []
    sin, cos = math.sin(a), math.cos(a)
    for x, y, z in fig:
        newfig.append((x*cos-y*sin, x*sin+y*cos, z))
    return newfig
```



Program structure

cube3d.py

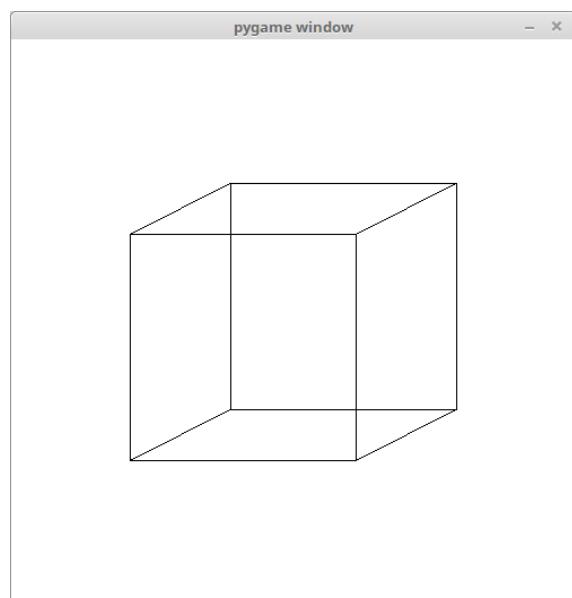
initialization

```
def drawline3d(...)  
def draw3d(...)  
def rotx(...)  
def roty(...)  
def rotz(...)
```

constants

cube definition

pygame loop



initialization

```
import pygame, sys, math  
black, white = (0, 0, 0), (255, 255, 255)  
  
pygame.init()  
scr = pygame.display.set_mode((500, 500))  
win = scr.get_rect()  
scr.fill(white)
```

pygame loop

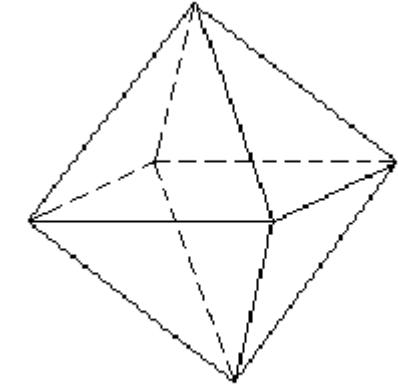
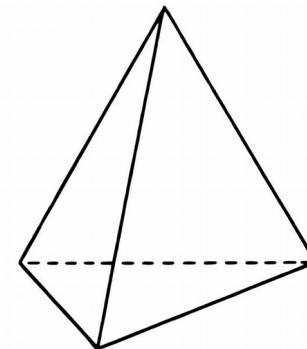
```
pygame.key.set_repeat(50,50)  
  
while True:  
    for event in pygame.event.get():  
        if event.type == pygame.QUIT:  
            sys.exit()  
        if event.type == pygame.KEYDOWN:  
            if event.key == pygame.K_x:  
                cube = rotx(cube, angle)  
            if event.key == pygame.K_y:  
                cube = roty(cube, angle)  
            if event.key == pygame.K_z:  
                cube = rotz(cube, angle)  
  
    scr.fill(white)  
    drawfigure3d(cube)  
    pygame.display.flip()
```



Exercise 1

- Define and display:

- tetrahedron
 - octahedron



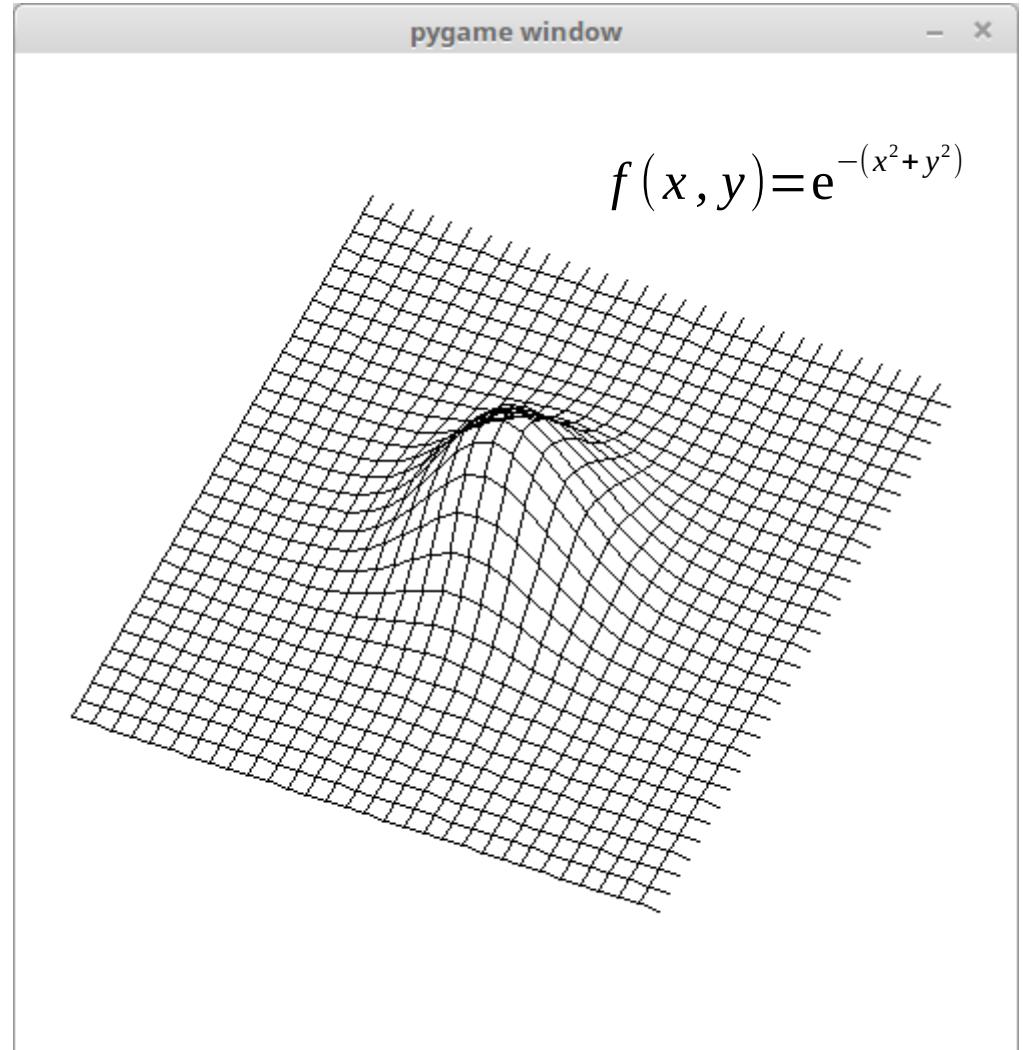
- Optionally:

- Implement backward rotation
 - Implement zoom
 - Implement translations (directional shifts)



3D function viewer

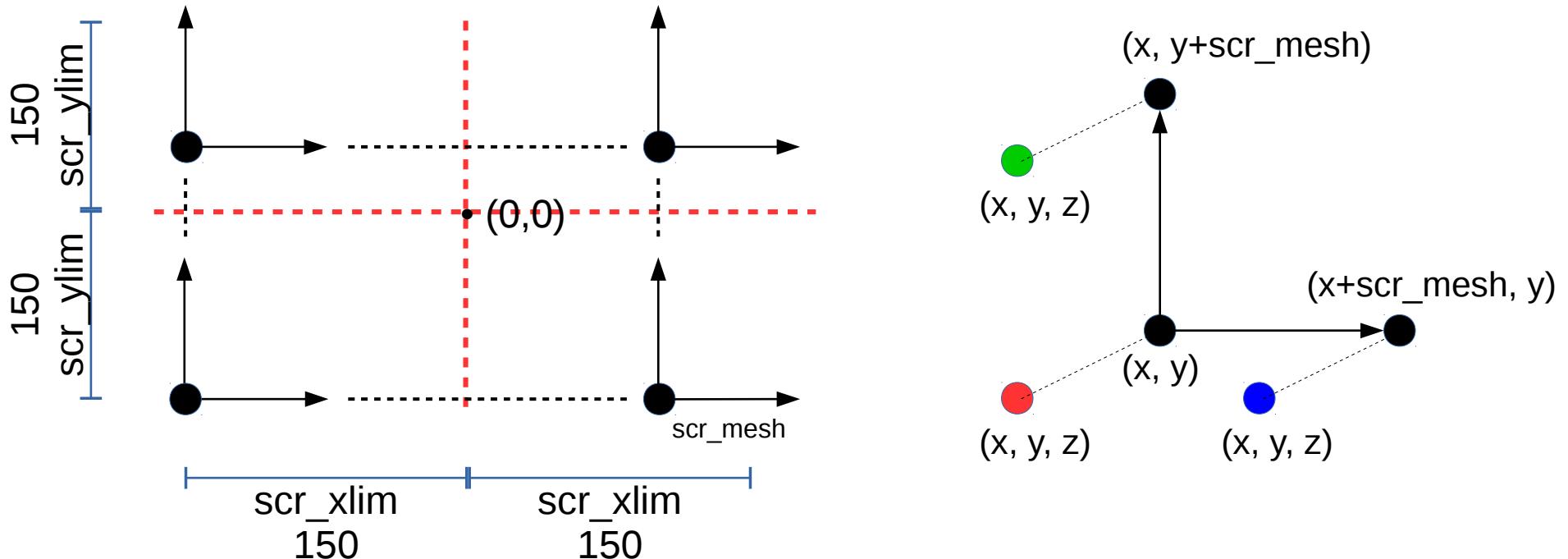
- define $z = f(x,y)$
- compute all (x,y,z) points and store 3D wire-mesh as segment-lines
- draw the wire-mesh with `drawfigure3D()`



```
z = math.exp(-((x)**2 + (y)**2))
```



Making (x,y,z) wire-mesh

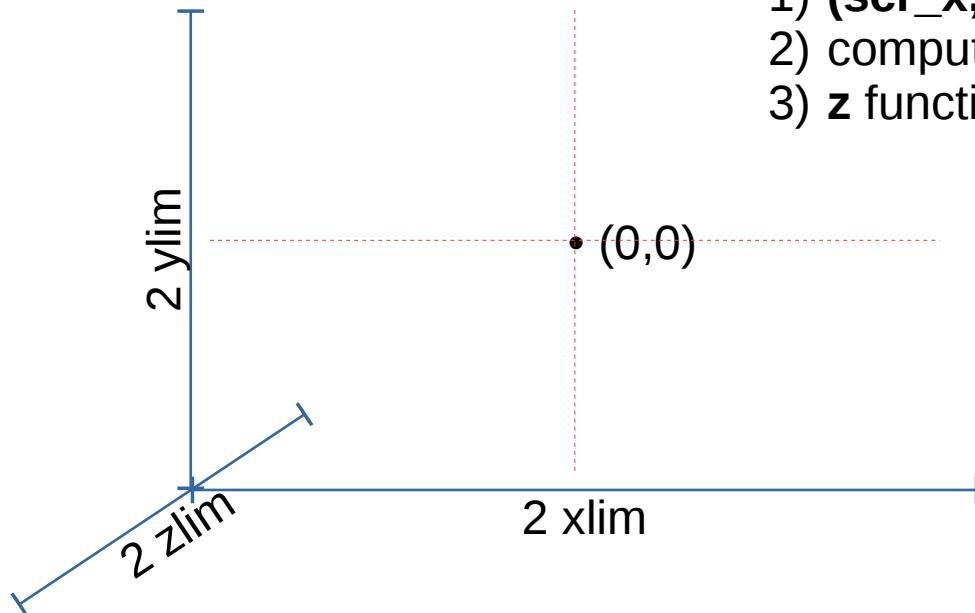


```
# drawing limits for screen - around (0,0)
scr_xlim, scr_ylim, scr_zlim = 150, 150, 150
scr_mesh = 10

# create function mesh
wiremesh = []
for x in range(-scr_xlim, scr_xlim, scr_mesh):
    for y in range(-scr_ylim, scr_ylim, scr_mesh):
        wiremesh.extend([(x,y,z(x,y)), (x+scr_mesh,y,z(x+scr_mesh,y))])
        wiremesh.extend([(x,y,z(x,y)), (x,y+scr_mesh,z(x,y+scr_mesh))])
```



Computing $z(x, y)$



- 1) (scr_x, scr_y) screen coord. $\rightarrow (x, y)$ function coords.
- 2) compute $z = f(x, y)$
- 3) z function coords $\rightarrow scr_z$ screen coord.

$$x = scr_x \frac{xlim}{scr_xlim}$$

$$y = scr_y \frac{ylim}{scr_ylim}$$

$$scr_z = z \frac{scr_zlim}{zlim}$$

```
# drawing limits for 3d space - around (0,0,0)
xlim, ylim, zlim = math.pi, math.pi, 1.0

def z(scr_x, scr_y):
    x = (float(scr_x) / scr_xlim) * xlim
    y = (float(scr_y) / scr_ylim) * ylim

    z = math.exp(-((x)**2 + (y)**2))

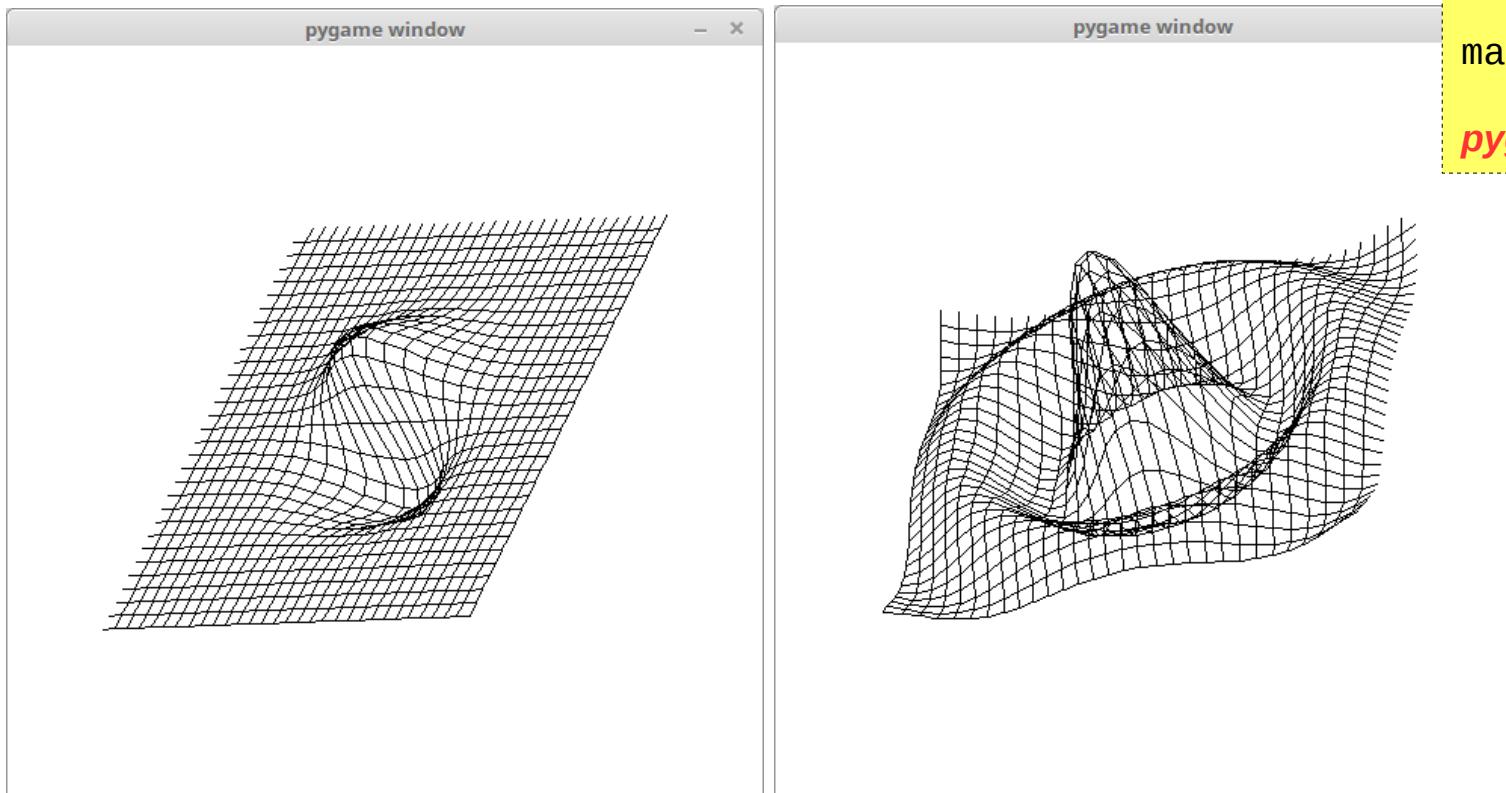
    return (z / zlim) * scr_zlim
```



Exercise 2

wiremesh3d.py

- Define and draw other 3D functions
- Optionally:
 - Draw the direction axes
 - Show the bounding box for drawing



initialization

```
def drawline3d(...)  
def drawfigure3d(...)  
def rotx(...)  
def roty(...)  
def rotz(...)  
def z(...):
```

constants

```
make wire-mesh
```

pygame loop